
Fides Documentation

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The Fides developers

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Source code: <https://github.com/Fides-dev/fides>

**CHAPTER
ONE**

ABOUT FIDES

Fides implements an Interior Trust Region Reflective for boundary constrained optimization problems based on the papers [ColemanLi1994] and [ColemanLi1996]. Accordingly, Fides is named after the Roman goddess of trust and reliability. In contrast to other optimizers, Fides solves the full trust -region subproblem exactly, which can yields higher quality proposal steps, but is computationally more expensive. This makes Fides particularly attractive for optimization problems with objective functions that are computationally expensive to evaluate and the computational cost of solving the trust -region subproblem is negligible.

1.1 Features

- Boundary constrained interior trust-region optimization
- Recursive Reflective and Truncated constraint management
- Full and 2D subproblem solution solvers
- BFGS, DFP and SR1 Hessian Approximations

FIDES PYTHON API

Modules

<code>fides</code>	Fides
<code>fides.minimize</code>	Minimization
<code>fides.trust_region</code>	Trust Region Step Evaluation
<code>fides.subproblem</code>	Subproblem Solvers
<code>fides.hessian_approximation</code>	Hessian Update Strategies
<code>fides.logging</code>	Logging
<code>fides.constants</code>	Constants

2.1 Fides

Fides is an interior trust-region reflective optimizer

2.2 Minimization

This module performs the optimization given a step proposal.

Classes Summary

<code>Optimizer(fun, ub, lb[, verbose, options, ...])</code>	Performs optimization
--	-----------------------

Classes

```
class fides.minimize.Optimizer(fun, ub, lb, verbose=10, options=None, funargs=None, hessian_update=None)
```

Performs optimization

Variables

- **fun** – Objective function
- **funargs** – Keyword arguments that are passed to the function
- **lb** – Lower optimization boundaries

- **ub** – Upper optimization boundaries
- **options** – Options that configure convergence checks
- **delta_iter** – Trust region radius that was used for the current step
- **delta** – Updated trust region radius
- **x** – Current optimization variables
- **fval** – Objective function value at x
- **grad** – Objective function gradient at x
- **x_min** – Optimal optimization variables
- **fval_min** – Objective function value at x_min
- **grad_min** – Objective function gradient at x_min
- **hess** – Objective function Hessian (approximation) at x
- **hessian_update** – Object that performs hessian updates
- **starttime** – Time at which optimization was started
- **iteration** – Current iteration
- **converged** – Flag indicating whether optimization has converged
- **exitflag** – ExitFlag to indicate reason for termination
- **verbose** – Verbosity level for logging
- **logger** – logger instance

__init__(fun, ub, lb, verbose=10, options=None, funargs=None, hessian_update=None)
Create an optimizer object

Parameters

- **fun** (`typing.Callable`) – This is the objective function, if no `hessian_update` is provided, this function must return a tuple (fval, grad), otherwise this function must return a tuple (fval, grad, Hessian)
- **ub** (`numpy.ndarray`) – Upper optimization boundaries. Individual entries can be set to np.inf for respective variable to have no upper bound
- **lb** (`numpy.ndarray`) – Lower optimization boundaries. Individual entries can be set to -np.inf for respective variable to have no lower bound
- **verbose** (`typing.Optional[int]`) – Verbosity level, pick from logging.[DEBUG,INFO,WARNING,ERROR]
- **options** (`typing.Optional[typing.Dict]`) – Options that control termination of optimization. See `minimize` for details.
- **funargs** (`typing.Optional[typing.Dict]`) – Additional keyword arguments that are to be passed to fun for evaluation
- **hessian_update** (`typing.Optional[fides.hessian_approximation.HessianApproximation]`) – Subclass of `fides.hessian_update.HessianApproximation` that performs the hessian updates in every iteration.

check_continue()

Checks whether minimization should continue based on convergence, iteration count and remaining computational budget

Return type `bool`

Returns flag indicating whether minimization should continue

check_convergence (`fval`, `x`, `grad`)

Check whether optimization has converged.

Parameters

- `fval` – updated objective function value
- `x` – updated optimization variables
- `grad` – updated objective function gradient

Return type `None`

check_finite (`grad=None`, `hess=None`)

Checks whether objective function value, gradient and Hessian (approximation) have finite values and optimization can continue.

Parameters

- `grad` (`typing.Optional[numumpy.ndarray]`) – gradient to be checked for finiteness, if not provided, current one will be checked
- `hess` (`typing.Optional[numumpy.ndarray]`) – Hessian (approximation) to be checked for finiteness, if not provided, current one will be checked

Raises `RuntimeError` if any of the variables have non-finite entries

check_in_bounds (`x=None`)

Checks whether the current optimization variables are all within the specified boundaries

Raises `RuntimeError` if any of the variables are not within boundaries

get_affine_scaling()

Computes the vector `v` and `dv`, the diagonal of it's Jacobian. For the definition of `v`, see Definition 2 in [Coleman-Li1994]

Return type `typing.Tuple[numumpy.ndarray, numumpy.ndarray]`

Returns `v` scaling vector `dv` diagonal of the Jacobian of `v` wrt `x`

log_header()

Prints the header for diagnostic information, should complement `Optimizer.log_step()`.

log_step (`accepted`, `step`, `fval`)

Prints diagnostic information about the current step to the log

Parameters

- `accepted` (`bool`) – flag indicating whether the current step was accepted
- `step` (`fides.steps.Step`) – proposal step
- `fval` (`float`) – new `fval` if step is accepted

log_step_initial()

Prints diagnostic information about the initial step to the log

make_non_degenerate (`eps=2.220446049250313e-14`)

Ensures that `x` is non-degenerate, this should only be necessary for initial points.

Parameters `eps` – degeneracy threshold

Return type `None`

minimize(*x0*)

Minimize the objective function the interior trust-region reflective algorithm described by [ColemanLi1994] and [ColemanLi1996]. Convergence with respect to function value is achieved when $|f_{k+1} - f_k| < \text{options}[f atol] - f_k$ $\text{options}[f rtol]$. Similarly, convergence with respect to optimization variables is achieved when $\|x_{k+1} - x_k\| < \text{options}[x atol] - x_k$ $\text{options}[x rtol]$. Convergence with respect to the gradient is achieved when $\|g_k\| < \text{options}[g atol]$ or $\|g_k\| < \text{options}[g rtol] * f_k$. Other than that, optimization can be terminated when iterations exceed $\text{options}[max iter]$ or the elapsed time is expected to exceed $\text{options}[max time]$ on the next iteration.

Parameters *x0* (`numpy.ndarray`) – initial guess

Returns *fval*: final function value, *x*: final optimization variable values, *grad*: final gradient, *hess*: final Hessian (approximation)

track_minimum(*x_new*, *fval_new*, *grad_new*)

Function that tracks the optimization variables that have minimal function value independent of whether the step is accepted or not.

Parameters

- *x_new* (`numpy.ndarray`) –
- *fval_new* (`float`) –
- *grad_new* (`numpy.ndarray`) –

Return type `None`

Returns

update(*step*, *x_new*, *fval_new*, *grad_new*, *hess_new=None*)

Update self according to employed step

Parameters

- *step* (`fides.steps.Step`) – Employed step
- *x_new* (`numpy.ndarray`) – New optimization variable values
- *fval_new* (`float`) – Objective function value at *x_new*
- *grad_new* (`numpy.ndarray`) – Objective function gradient at *x_new*
- *hess_new* (`typing.Optional[numpy.ndarray]`) – (Approximate) objective function Hessian at *x_new*

Return type `None`

update_tr_radius(*fval*, *grad*, *step*, *dv*)

Update the trust region radius

Parameters

- *fval* (`float`) – new function value if step defined by *step_sx* is taken
- *grad* (`numpy.ndarray`) – new gradient value if step defined by *step_sx* is taken
- *step* (`fides.steps.Step`) – step
- *dv* (`numpy.ndarray`) – derivative of scaling vector *v* wrt *x*

Return type `bool`

Returns flag indicating whether the proposed step should be accepted

2.3 Trust Region Step Evaluation

This module provides the machinery to evaluate different trust-region(-reflective) step proposals and select among them based on to their performance according to the quadratic approximation of the objective function

Functions Summary

<code>trust_region(x, g, hess, scaling, delta, dv, ...)</code>	Compute a step according to the solution of the trust-region subproblem.
--	--

Functions

`fides.trust_region.trust_region(x, g, hess, scaling, delta, dv, theta, lb, ub, subspace_dim, stepback_strategy, refine_stepback, logger)`

Compute a step according to the solution of the trust-region subproblem. If step-back is necessary, gradient and reflected trust region step are also evaluated in terms of their performance according to the local quadratic approximation

Parameters

- `x` (`numpy.ndarray`) – Current values of the optimization variables
- `g` (`numpy.ndarray`) – Objective function gradient at `x`
- `hess` (`numpy.ndarray`) – (Approximate) objective function Hessian at `x`
- `scaling` (`scipy.sparse.csc.csc_matrix`) – Scaling transformation according to distance to boundary
- `delta` (`float`) – Trust region radius, note that this applies after scaling transformation
- `dv` (`numpy.ndarray`) – derivative of scaling transformation
- `theta` (`float`) – parameter regulating stepback
- `lb` (`numpy.ndarray`) – lower optimization variable boundaries
- `ub` (`numpy.ndarray`) – upper optimization variable boundaries
- `subspace_dim` (`fides.constants.SubSpaceDim`) – Subspace dimension in which the subproblem will be solved. Larger subspaces require more compute time but can yield higher quality step proposals.
- `stepback_strategy` (`fides.constants.StepBackStrategy`) – Strategy that is applied when the proposed step exceeds the optimization boundary.
- `refine_stepback` (`bool`) – If set to True, proposed steps that are computed via the specified stepback_strategy will be refined via optimization.
- `logger` (`logging.Logger`) – `logging.Logger` instance to be used for logging

Return type `fides.steps.Step`

Returns s: proposed step, ss: rescaled proposed step, qpval: expected function value according to local quadratic approximation, subspace: computed subspace for reuse if proposed step is not accepted, steptype: type of step that was selected for proposal

2.4 Subproblem Solvers

This module provides the machinery to solve 1- and N-dimensional trust-region subproblems.

Functions Summary

<code>dsecular(lam, w, eigvals, eigvecs, delta)</code>	Derivative of the secular equation
<code>dslam(lam, w, eigvals, eigvecs)</code>	Computes the derivative of the solution $s(\lambda)$ with respect to lambda, where s is the ubproblem solution according to
<code>secular(lam, w, eigvals, eigvecs, delta)</code>	Secular equation
<code>slam(lam, w, eigvals, eigvecs)</code>	Computes the solution $s(\lambda)$ as subproblem solution according to
<code>solve_1d_trust_region_subproblem(B, g, s, ...)</code>	Solves the special case of a one-dimensional subproblem
<code>solve_nd_trust_region_subproblem(B, g, delta)</code>	This function exactly solves the n-dimensional subproblem.

Functions

`fides.subproblem.dsecular(lam, w, eigvals, eigvecs, delta)`

Derivative of the secular equation

$$\phi(\lambda) = \frac{1}{\|s\|} - \frac{1}{\Delta}$$

with respect to λ

Parameters

- `lam` (`float`) – λ
- `w` (`numpy.ndarray`) – precomputed eigenvector coefficients for $-g$
- `eigvals` (`numpy.ndarray`) – precomputed eigenvalues of B
- `eigvecs` (`numpy.ndarray`) – precomputed eigenvectors of B
- `delta` (`float`) – trust region radius Δ

Returns $\frac{\partial \phi(\lambda)}{\partial \lambda}$

`fides.subproblem.dslam(lam, w, eigvals, eigvecs)`

Computes the derivative of the solution $s(\lambda)$ with respect to lambda, where s is the ubproblem solution according to

$$-(B + \lambda I)s = g$$

Parameters

- `lam` (`float`) – λ
- `w` (`numpy.ndarray`) – precomputed eigenvector coefficients for $-g$
- `eigvals` (`numpy.ndarray`) – precomputed eigenvalues of B
- `eigvecs` (`numpy.ndarray`) – precomputed eigenvectors of B

Returns $\frac{\partial s(\lambda)}{\partial \lambda}$

`fides.subproblem.secular(lam, w, eigvals, eigvecs, delta)`

Secular equation

$$\phi(\lambda) = \frac{1}{\|s\|} - \frac{1}{\Delta}$$

Subproblem solutions are given by the roots of this equation

Parameters

- `lam` (`float`) – λ
- `w` (`numpy.ndarray`) – precomputed eigenvector coefficients for $-g$
- `eigvals` (`numpy.ndarray`) – precomputed eigenvalues of B
- `eigvecs` (`numpy.ndarray`) – precomputed eigenvectors of B
- `delta` (`float`) – trust region radius Δ

Returns $\phi(\lambda)$

`fides.subproblem.slam(lam, w, eigvals, eigvecs)`

Computes the solution $s(\lambda)$ as subproblem solution according to

$$-(B + \lambda I)s = g$$

Parameters

- `lam` (`float`) – λ
- `w` (`numpy.ndarray`) – precomputed eigenvector coefficients for $-g$
- `eigvals` (`numpy.ndarray`) – precomputed eigenvalues of B
- `eigvecs` (`numpy.ndarray`) – precomputed eigenvectors of B

Return type `numpy.ndarray`

Returns $s(\lambda)$

`fides.subproblem.solve_1d_trust_region_subproblem(B, g, s, delta, s0)`

Solves the special case of a one-dimensional subproblem

Parameters

- `B` (`numpy.ndarray`) – Hessian of the quadratic subproblem
- `g` (`numpy.ndarray`) – Gradient of the quadratic subproblem
- `s` (`numpy.ndarray`) – Vector defining the one-dimensional search direction
- `delta` (`float`) – Norm boundary for the solution of the quadratic subproblem
- `s0` (`numpy.ndarray`) – reference point from where search is started, also counts towards norm of step

Return type `numpy.ndarray`

Returns Proposed step-length

`fides.subproblem.solve_nd_trust_region_subproblem(B, g, delta, logger=None)`

This function exactly solves the n-dimensional subproblem.

$$\operatorname{argmin}_s \{s^T B s + s^T g = 0 : \|s\| \leq \Delta, s \in \mathbb{R}^n\}$$

The solution to is characterized by the equation $-(B + \lambda I)s = g$. If B is positive definite, the solution can be obtained by $\lambda = 0$ if $Bs = -g$ satisfies $\|s\| \leq \Delta$. If B is indefinite or $Bs = -g$ satisfies $\|s\| > \Delta$ and an appropriate λ has to be identified via 1D rootfinding of the secular equation

$$\phi(\lambda) = \frac{1}{\|s(\lambda)\|} - \frac{1}{\Delta} = 0$$

with $s(\lambda)$ computed according to an eigenvalue decomposition of B . The eigenvalue decomposition, although being more expensive than a cholesky decomposition, has the advantage that eigenvectors are invariant to changes in λ and eigenvalues are linear in λ , so factorization only has to be performed once. We perform the linesearch via Newton's algorithm and Brent-Q as fallback. The hard case is treated separately and serves as general fallback.

Parameters

- **B** (`numpy.ndarray`) – Hessian of the quadratic subproblem
- **g** (`numpy.ndarray`) – Gradient of the quadratic subproblem
- **delta** (`float`) – Norm boundary for the solution of the quadratic subproblem
- **logger** (`typing.Optional[logging.Logger]`) – Logger instance to be used for logging

Return type `typing.Tuple[numpy.ndarray, str]`

Returns s: Selected step, step_type: Type of solution that was obtained

2.5 Hessian Update Strategies

This module provides various generic Hessian approximation strategies that can be employed when calculating the exact Hessian or an approximation is computationally too demandind.

Classes Summary

<code>BFGS</code> ([hess_init])	Broyden-Fletcher-Goldfarb-Shanno update strategy.
<code>DFP</code> ([hess_init])	Davidon-Fletcher-Powell update strategy.
<code>HessianApproximation</code> ([hess_init])	Abstract class from which Hessian update strategies should subclass
<code>SR1</code> ([hess_init])	Symmetric Rank 1 update strategy.

Classes

```
class fides.hessian_approximation.BFGS (hess_init=None)
Broyden-Fletcher-Goldfarb-Shanno update strategy. This is a rank 2 update strategy that always yields positive-semidefinite hessian approximations.
```

```
class fides.hessian_approximation.DFP (hess_init=None)
Davidon-Fletcher-Powell update strategy. This is a rank 2 update strategy that always yields positive-semidefinite hessian approximations. It usually does not perform as well as the BFGS strategy, but included for the sake of completeness.
```

```
class fides.hessian_approximation.HessianApproximation (hess_init=None)
Abstract class from which Hessian update strategies should subclass
```

```
__init__ (hess_init=None)
Create Hessian update strategy instance
```

Parameters `hess_init` (`typing.Optional[numpy.ndarray]`) – Initial guess for the Hessian, if empty Identity matrix will be used

```
get_mat()
    Getter for the Hessian approximation :rtype: numpy.ndarray :return:

init_mat(dim)
    Initializes this approximation instance and checks the dimensionality

Parameters dim(int) – dimension of optimization variables

class fides.hessian_approximation.SR1(hess_init=None)
    Symmetric Rank 1 update strategy. This updating strategy may yield indefinite hessian approximations.
```

2.6 Logging

This module provides the machinery that is used to display progress of the optimizer as well as debugging information

var logger logging.Logger instance that can be used throughout fides

Functions Summary

<code>create_logger(level)</code>	Creates a logger instance.
-----------------------------------	----------------------------

Functions

`fides.logging.create_logger(level)`
Creates a logger instance. To avoid unnecessary locks during multithreading, different logger instance should be created for every

Parameters level(int) – logging level
Return type logging.Logger
Returns logger instance

2.7 Constants

This module provides a central place to define native python enums and constants that are used in multiple other modules

Classes Summary

<code>ExitFlag(value)</code>	Defines possible exitflag values for the optimizer to indicate why optimization exited.
<code>Options(value)</code>	Defines all the fields that can be specified in Options to Optimizer
<code>StepBackStrategy(value)</code>	Defines the possible choices of search refinement if proposed step reaches optimization boundary
<code>SubSpaceDim(value)</code>	Defines the possible choices of subspace dimension in which the subproblem will be solved.

Classes

```
class fides.constants.ExitFlag (value)
    Defines possible exitflag values for the optimizer to indicate why optimization exited. Negative value indicate errors while positive values indicate convergence.

    DID_NOT_RUN = 0
        Optimizer did not run

    EXCEEDED_BOUNDARY = -4
        Exceeded specified boundaries

    FTOL = 1
        Converged according to fval difference

    GTOL = 3
        Converged according to gradient norm

    MAXITER = -1
        Reached maximum number of allowed iterations

    MAXTIME = -2
        Expected to reach maximum allowed time in next iteration

    NOTFINITE = -3
        Encountered non-finite fval/grad/hess

    XTOL = 2
        Converged according to x difference

class fides.constants.Options (value)
    Defines all the fields that can be specified in Options to Optimizer

    DELTA_INIT = 'delta_init'
        initial trust region radius

    FATOL = 'f atol'
        absolute tolerance for convergence based on fval

    FRTOL = 'fr tol'
        relative tolerance for convergence based on fval

    GATOL = 'g atol'
        absolute tolerance for convergence based on grad

    GRTOL = 'gr tol'
        relative tolerance for convergence based on grad

    MAXITER = 'maxiter'
        maximum number of allowed iterations

    MAXTIME = 'maxtime'
        maximum amount of walltime in seconds

    STEPBACK_STRAT = 'stepback_strategy'
        method to use for stepback

    SUBSPACE_DIM = 'subspace_solver'
        trust region subproblem subspace

    THETA_MAX = 'theta_max'
        maximal fraction of step that would hit bounds
```

```
XATOL = 'xatol'
absolute tolerance for convergence based on x

XRTOL = 'xrtol'
relative tolerance for convergence based on x

class fides.constants.StepBackStrategy(value)
Defines the possible choices of search refinement if proposed step reaches optimization boundary

MIXED = 'mixed'
mix reflections and truncations

REFLECT = 'reflect'
recursive reflections at boundary

SINGLE_REFLECT = 'reflect_single'
single reflection at boundary

TRUNCATE = 'truncate'
truncate step at boundary and resolve subproblem

class fides.constants.SubSpaceDim(value)
Defines the possible choices of subspace dimension in which the subproblem will be solved.

FULL = 'full'
Full  $\mathbb{R}^n$ 

TWO = '2D'
Two dimensional Newton/Gradient subspace
```

**CHAPTER
THREE**

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